

Q :

$$ans(x) \leftarrow a(x, x), a(x, r)$$

$$\begin{array}{ccc} \uparrow : a & A & B \\ \hline & \cancel{A} & \cancel{B} \\ & 2 & 1 \end{array}$$

$$Q(\underline{I}) = \{1\}$$

$$Q' \quad ans(x) \leftarrow a(x, x)$$

$$Q \supseteq Q'$$

$$Q' \supseteq Q$$

$$Q: a \cup s(x) \leftarrow a(x, x), a(x, r)$$

$$Q': a \cup r(x) \leftarrow a(x, r)$$

$$Q' \subseteq Q \text{ trivial.}$$

$$Q \supseteq Q' \text{ ?}$$

$$Q: \text{ans}(x) \leftarrow a(x, x), a(x, y)$$

$$Q': \text{ans}(A) \leftarrow a(A, A)$$

$$Q \subseteq Q'$$

$$Q' \subseteq Q \text{ ?}$$

mapping from vars \cup cons of

$$Q \text{ to vars } \cup \text{ cons to } Q'$$

\emptyset	x	y	$a(x, x)$
	A	A	$\rightarrow a(A, A)$
			$a(\cancel{x}, y)$

\emptyset is a cont. map.

$$\begin{aligned} &\rightarrow a(A, A) \\ \emptyset(\text{ans}(x)) & \\ &\rightarrow \text{ans}(A) \end{aligned}$$

$$Q: ahs(x) \leftarrow a(x, x), a(*, *)$$

$$Q': ahs(x) \leftarrow a(x, x)$$

$$Q' \not\equiv Q$$

$$\begin{array}{c} \uparrow \\ a \quad A \quad B \\ \hline \quad \uparrow \quad \uparrow \end{array}$$

$$Q(\uparrow) = \emptyset$$

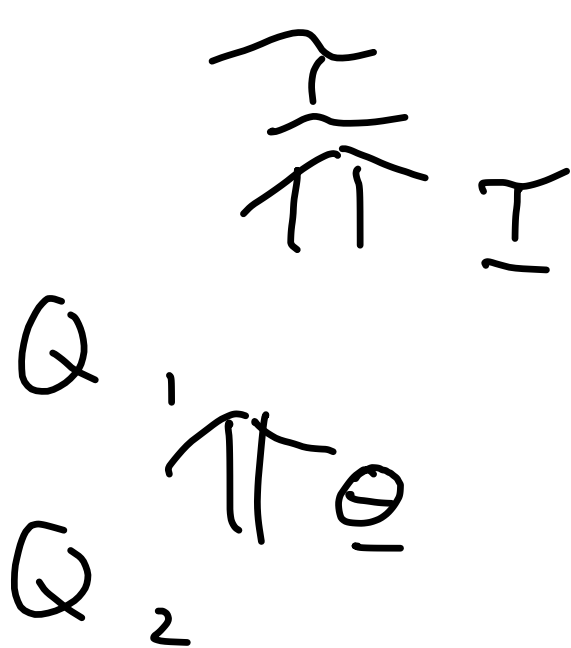
$$Q'(\uparrow) = \{ \uparrow \}$$

$O(n) ?$

Q 1 : n vars

Q 2 : $\uparrow\uparrow$
 ~~m~~ vars.

Q 1 \equiv Q 2



$$\mu = T(\vec{U})$$

$$\mu = \tau'(\vec{V})$$

$$Q: \text{ans}(x) \leftarrow a(x, x), a(x, \gamma)$$

$$Q': \text{ans}(A) \leftarrow a(A, A)$$

$$\frac{\theta \quad x \quad \gamma}{A \quad A}$$

is a cont.
mapping.

$$\tilde{\tau}: \frac{a \quad A \quad B}{1 \quad 1}$$

$$\frac{\mu \in Q'(\mathcal{I})}{\mu: 1}$$

$$\tau: A \rightarrow 1$$

to prove:

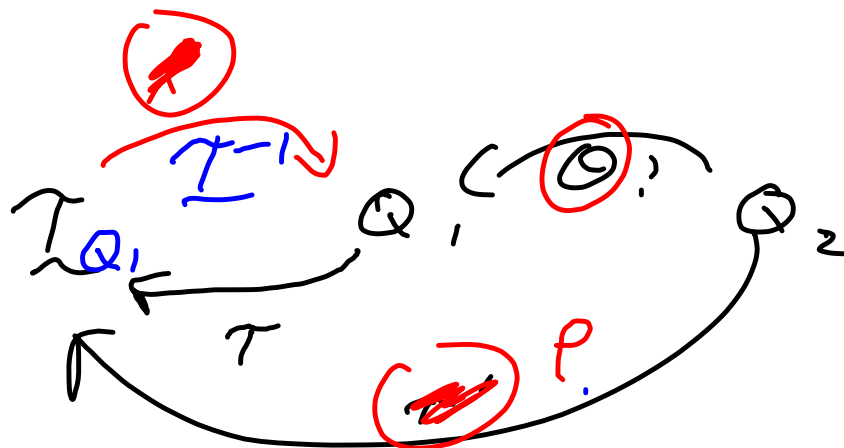
$$\mu \in Q(\mathcal{I})$$

$$\mu \in \tau'(\text{ans}(x))$$

$$\tau' = x \rightarrow 1, \gamma \rightarrow 1$$

Ass. $Q_1 \subseteq Q_2$

we have to find a containment
mapping Θ from Q_2 to Q_1



$T: x \rightarrow 1$ T^{-1} does not
 $y \rightarrow 1$ exist.

T is a one-one mapping.

T^{-1} is also a mapping.

